

2.

$$2(f) \text{ (cont.) } y' = \frac{2(3x-2) - (2x+5)3}{(3x-2)^2}$$

Now simplify, but carefully:  $3x-2$  is not a common factor in the numerator.

$$y' = -19/(3x-2)^2.$$

$$2(g) \ y = \sqrt{4x^2+2} = (4x^2+2)^{1/2} \quad (\text{exponential form is best for roots})$$

$$y' = \frac{1}{2}(4x^2+2)^{-1/2} \cdot (4x^2+2)' \quad [\text{Chain Rule}]$$

$$= 4x^2 / \sqrt{4x^2+2}$$

3.  $x^2 + 4xy - 2y^2 = 5$ . Differentiate with respect to  $x$ , noting that  $y$  is a function of  $x$

$$\frac{d}{dx}(x^2) + 4 \frac{d}{dx}(xy) - 2 \frac{d}{dx}(y^2) = \frac{d}{dx}(5)$$

$$2x + 4 \left( \frac{dx}{dx} y + x \frac{dy}{dx} \right) - 2 \frac{d(y^2)}{dy} \frac{dy}{dx} = 0$$

product rule chain rule!

$$2x + 4(1 \cdot y + x \frac{dy}{dx}) - 2 \cdot 2y \frac{dy}{dx} = 0$$

Collect  $\frac{dy}{dx}$  terms & solve for it:

$$\frac{dy}{dx}(4x - 4y) + 2x + 4y = 0$$

$$\frac{dy}{dx} = \frac{2x + 4y}{4y - 4x} = \boxed{\frac{x + 2y}{2y - 2x}}$$